

**Note taking guide: Solving equations with variables on both sides of the equal sign**

**Example 1:**  $3x + 7 = 2x + 20$

Bar Model	Decompose	Traditional
$3x + 7 = 2x + 20$ <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div>	$+ = +$	$+ = +$  <b>#1</b>     <b>#2</b>

**“You Try” for Example 1:**  $4x + 8 = 5x + 3$

**Solution**

Bar Model	Decompose	Traditional
$4x + 8 = 5x + 3$ <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div> <div style="border: 1px solid black; height: 20px; width: 100%; margin-bottom: 5px;"></div>		

**Note taking guide: Solving equations with variables on both sides of the equal sign**

**Example 2:**  $x + \quad = x + \quad$

<b>Bar Model</b>	<b>Decompose</b>	<b>Traditional</b>
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**Note taking guide: Solving equations with variables on both sides of the equal sign**

**Example 3:**  $5 + 3 + 2 = 7 + 4$

Bar Model	Decompose	Traditional
<p style="text-align: center;"><math>5 + 3 + 2 = 7 + 4</math></p> <div style="border: 1px solid black; width: 250px; height: 20px; margin-bottom: 5px;"></div> <div style="border: 1px solid black; width: 250px; height: 20px; margin-bottom: 5px;"></div> <div style="border: 1px solid black; width: 250px; height: 20px; margin-bottom: 5px;"></div> <div style="border: 1px solid black; width: 250px; height: 20px; margin-bottom: 5px;"></div>	<p><math>5 + 3 + 2 = 7 + 4</math></p>	<p><math>5 + 3 + 2 = 7 + 4</math></p>

**“You Try” for Example 3:**  $x + x = x + x$

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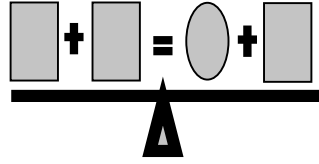




# Balance Beam Game

*This game can be played the day before teaching Solving variables on both sides to introduce the idea of removing from both sides.*

Say, "Let's play a game" Write on board.



Say, "Can you tell me what circle is equal to?"

Answer, "One square"

"Fabulous!"

*Discuss the "sides" of the balance and relate to the equal sign. Good time to review*

Say, "Let's try this one." ~~irrcrci~~, irc its td

**\*\*Optional if time allows or to have another example: Say, “Now let’s try one more.”**

*Write*

Please note that this lesson is designed for a block schedule period. If you have a traditional period you complete this lesson over the course of two days.

You’ll notice throughout this lesson that we are working horizontally not vertically. We’ve seen that this alleviates many issues that come up.

We also want you to notice the common occurrences in all the three methods. Point them out to your students or have them point them out to you.

We want them to do the other methods so that they gain a better understanding of the traditional method. Over time we want them to do the traditional method.

## Warm up

*Debrief all problems except “other” this will be the beginning of the lesson.*

*Begin debriefing the last question*

*Write on board.*

$$2 + 3 = 20$$

$$x = x +$$

*Say*



Say, "If we take that solution and substitute that into the second equation, we get"

**BOARD**

$$2 + 3 = 20$$

Variables are on the same side

=

=

$$x = x +$$

Variables on both sides

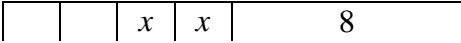
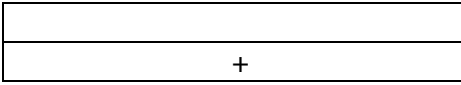


After sufficient time for students to complete and/or for you to circulate write the solution

**Solution**

<b>Bar Model</b>	<b>Decompose</b>	<b>Traditional</b>
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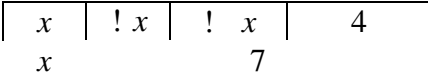
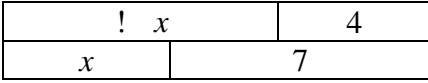
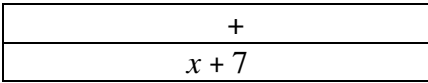
4 8 5 3



**Example 2:**  $2x + 4 = x + 7$

Bar Model	Decompose	Traditional
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$2x + 4 = x + 7$



**“You Try” for Example 2:**  $-2 - 4 = -3 + 3$

After sufficient time for students to complete and/or for you to circulate write the solution

**Solution**

Bar Model	Decompose	Traditional						
$x = x +$	$x = x +$	$2 \quad 4 \quad 3 \quad 3$						
<table border="1" style="margin: 5px auto; border-collapse: collapse;"> <tr><td style="text-align: center; padding: 5px;"><math>2x \quad 4</math></td></tr> <tr><td style="text-align: center; padding: 5px;"><math>x</math></td></tr> </table>	$2x \quad 4$	$x$	$x = x + \quad x +$ $= x +$ $+ \quad + = x +$ $+ = x$ $= x$ $= x$ $x =$	$2 \quad 3 \quad 4 \quad 3 \quad 3 \quad 3$ $4 \quad 3$ $4 \quad 4 \quad 3 \quad 4$				
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$x$								
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- 7								
-								
$! = !7$ $= 7$								



**“You Try” for Example 3:**  $x \quad x! \quad x$

*After sufficient time for students to complete and/or for you to circulate write the solution.*

**Solution**

Bar Model	Decompose	Traditional
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$x \quad x! \quad x$

6	5
4	!5 + 2

$x$	5
4x	5      2x

$x$	5
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$x$

**Example 4:**

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**“You Try” for Example 4:**  $x! + x = x! ! x$

*After sufficient time for students to complete and/or for you to circulate write the solution.*

**Solution**

<b>Bar Model</b>	<b>Decompose</b>	<b>Traditional</b>						
$\begin{array}{ c c c } \hline & ! & ! \\ \hline 4x & 2 & 3x \\ \hline 11 & 2 & 4 \\ \hline \end{array}$								
<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="width: 33%;"></td> <td style="width: 33%; text-align: center;">! 2</td> <td style="width: 33%; text-align: center;">3x</td> </tr> <tr> <td style="text-align: center;">11x</td> <td></td> <td style="text-align: center;">! 4</td> </tr> </table>		! 2	3x	11x		! 4		
	! 2	3x						
11x		! 4						
<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="width: 66%; text-align: center;"><math>4x + 3x</math></td> <td style="width: 33%; text-align: center;">! 2</td> </tr> <tr> <td style="text-align: center;"><math>11x \quad 4x</math></td> <td></td> </tr> </table>	$4x + 3x$	! 2	$11x \quad 4x$					
$4x + 3x$	! 2							
$11x \quad 4x$								
<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="width: 66%;"></td> <td style="width: 33%; text-align: center;">! 2</td> </tr> <tr> <td></td> <td></td> </tr> </table>		! 2						
	! 2							



**“You Try” for Example 5:**  $2(3) + 4 = 10$

*After sufficient time for students to complete and/or for you to circulate write the solution.*

**Solution**

**Bar Model**

**Decompose**

**Notice throughout this lesson that we are working horizontally not vertically. We've seen that this alleviates many of the issues that come up.**

**Notice the common occurrences in all the three methods. Point them out to your students or have them point them out to you.**

**We want them to do the other methods so that they gain a better understanding of the traditional method. Over time we want them to do the traditional method.**

**NOTE:**

**Homework**

**To incorporate the multiple methods it is highly encouraged to assign fewer problems to be done multiple ways.**